# A Kinetic Model of the Hydrogen Assisted Selective Catalytic Reduction of NO with Ammonia over Ag/Al<sub>2</sub>O<sub>3</sub>

# Stefanie Tamm and Louise Olsson

Competence Centre for Catalysis, Chalmers University of Technology, 412 96 Göteborg, Sweden Chemical Reaction Engineering, Chalmers University of Technology, 412 96 Göteborg, Sweden

# Sebastian Fogel

Haldor Topsøe A/S, Nymøllevej 55, 2800 Kgs. Lyngby, Denmark

Center for Individual Nanoparticle Functionality (CINF), Dept. of Physics, Technical University of Denmark, Fysikvej 307, 2800 Kgs. Lyngby, Denmark

### Pär Gabrielsson

Haldor Topsøe A/S, Nymöllevej 55, 2800 Kgs. Lyngby, Denmark

### Magnus Skoglundh

Competence Centre for Catalysis, Chalmers University of Technology, 412 96 Göteborg, Sweden Applied Surface Chemistry, Chalmers University of Technology, SE-412 96 Göteborg, Sweden

DOI 10.1002/aic.14170 Published online July 15, 2013 in Wiley Online Library (wileyonlinelibrary.com)

A global kinetic model which describes  $H_2$ -assisted  $NH_3$ -SCR over an  $Ag/Al_2O_3$  monolith catalyst has been developed. The intention is that the model can be applied for dosing  $NH_3$  and  $H_2$  to an  $Ag/Al_2O_3$  catalyst in a real automotive application as well as contribute to an increased understanding of the reaction mechanism for  $NH_3$ -SCR. Therefore, the model needs to be simple and accurately predict the conversion of  $NO_x$ . The reduction of NO is described by a global reaction, with a molar stoichiometry between NO,  $NH_3$  and  $H_2$  of 1:1:2. Further reactions included in the model are the oxidation of  $NH_3$  to  $N_2$  and NO, oxidation of  $H_2$ , and the adsorption and desorption of  $NH_3$ . The model was fitted to the results of an  $NH_3$ -TPD experiment, an  $NH_3$  oxidation experiment, and a series of  $H_2$ -assisted  $NH_3$ -SCR steady-state experiments. The model predicts the conversion of  $NO_x$  well even during transient experiments. © 2013 American Institute of Chemical Engineers  $AIChE\ J$ , 59: 4325–4333, 2013

# Keywords: $NH_3$ -SCR, $NO_x$ reduction, $H_2$ , global kinetic model, $Ag/Al_2O_3$

# Introduction

The reduction of nitrogen oxides (NO<sub>x</sub>) in an oxidizing environment of the exhaust of a diesel or lean burn gasoline engine is one of the most challenging tasks for the catalytic converter in a vehicle. Moreover, exhaust gas temperatures have decreased during the last years due to more efficient utilization of the fuel in the engine. This leads to a demand of catalysts which are active for NO<sub>x</sub> reduction below 200°C. Nitrogen oxides can be efficiently reduced by selective catalytic reduction with ammonia (NH<sub>3</sub>-SCR). Different copper and iron exchanged zeolites have been studied for this application during the last decades. Hore recently it was shown that also Ag/Al<sub>2</sub>O<sub>3</sub> shows very good activity for the NH<sub>3</sub>-SCR reaction, reaching close to 100% NO<sub>x</sub> conversion at 200°C. In contrast to the zeolite-based catalysts,

© 2013 American Institute of Chemical Engineers

hydrogen is essential for efficient  $NH_3$ -SCR over  $Ag/Al_2O_3$ . Although the  $H_2$ -effect is known from the SCR reaction with hydrocarbons over  $Ag/Al_2O_3^{8-10}$  this effect is still not fully understood and a number of different mechanisms have been proposed, e.g., an increase of the number of active species, 11,12 reduction of silver, 9,13,14 increased amount of surface species 15-17 and removal of nitrates. 13,17-21 Recently, we showed that the presence of  $H_2$  facilitates the oxidation of nitrites to nitrates and, moreover, influences how the nitrates preferentially are bound to the surface. In the presence of  $H_2$ , there is a defined ratio between  $H_2$  in the presence of  $H_3$  and  $H_2$  occurs. This ratio is explained by hydrogen selectively removing single-oxygen atoms from the active silver sites, freeing the sites for  $H_3$  and  $H_3$  adsorption.

Based on the proposed reaction mechanism, kinetic models have been developed. Several detailed kinetic models have been developed for a variety of different SCR catalysts to increase the understanding of the reaction mechanism. <sup>2,19,24–27</sup> Moreover, such a model can be used as a tool in the

Correspondence concerning this article should be addressed to L. Olsson at Louise.Olsson@chalmers.se.

development of the complex exhaust gas after-treatment system of a vehicle, which may contain additional catalysts, for example, a diesel oxidation catalyst (DOC). Finally, a model is needed for the dosing strategy of the reducing agent. This model needs to accurately predict the NO<sub>x</sub> conversion as a function of the temperature, the surface coverage of important species, especially the reducing agent, and the concentration in the gas phase of the reducing agent. Furthermore, a model of H<sub>2</sub>-assisted NH<sub>3</sub>-SCR over Ag/Al<sub>2</sub>O<sub>3</sub> needs even to describe the H<sub>2</sub> concentration.

In the literature there are several kinetic models for Ag/Al<sub>2</sub>O<sub>3</sub> catalysts. <sup>19,28–30</sup> However, these models all describe hydrocarbon SCR (HC—SCR). The objective of this study is to develop a simple global kinetic model for H<sub>2</sub>-assisted NH<sub>3</sub>-SCR over an Ag/Al<sub>2</sub>O<sub>3</sub> catalyst, which can be used for the dosing strategy of NH<sub>3</sub> and H<sub>2</sub>. This model is based on the knowledge available for the reaction mechanism and on flow reactor experiments performed using a monolith catalyst, where the concentrations of all important gaseous compounds are varied. Most of the experimental results have already been reported previously. <sup>23</sup> However, to keep the model simple, only the most important reactions are included in the model and also the number of included species is limited.

# **Experimental Methods**

A presulfated Ag/Al<sub>2</sub>O<sub>3</sub> monolith catalyst with 6 wt% silver was used in the study. A higher amount of silver is needed to compensate for the loss of activity caused by sulfate formation. A catalyst in a real application will continuously be exposed to small amounts of sulfur from the fuel and lubricants. By presulfation we account for this sulfur exposure. More details about the preparation and properties of the catalyst can be found elsewhere.<sup>23</sup> Catalytic activity tests were performed in a horizontally mounted quartz tube flow reactor designed for monolithic catalyst samples. The quartz tube was externally heated by a heating coil and the monolith was placed in the end of the heated zone. The temperature of the reactor was measured inside a center channel of the monolith sample and controlled in the gas stream 10 mm before the monolith. Gases were supplied by separate mass flow controllers and water was added by a controlled evaporation and mixing system (all Bronkhorst Hi-Tech). The outlet gas composition was continuously analyzed using a gas phase FTIR spectrometer (mks-instruments, Multi-Gas2030) with the gas cell heated to 191°C and by mass spectrometry (Hiden HPR-20 QIC).

All activity tests were performed with a total flow of 3,500 mL/min, resulting in a GHSV of 33,100  $h^{-1}$ . The fresh catalyst was first activated for 5 min at 670°C in 5% water and then degreened in 250 ppm NO, 250 ppm NH<sub>3</sub>, 10% O<sub>2</sub> and 5% H<sub>2</sub>O in Ar at 600°C for 3 h. In each subsequent experiment the sample was initially pretreated in a flow of 10% O<sub>2</sub> in Ar at 500°C for 20 min. Afterward, the catalyst was cooled in 5% water in Ar to 70°C, where it was exposed to the reaction mixture for 40 min. Then, the temperature was increased in 8 steps at 20°C/min to 500°C (100, 150, 200, 250, 300 and 400°C). Each step lasted at least 20 min to obtain steady-state conditions. For temperature programmed desorption (TPD) experiments, the catalyst was cooled to 100°C in 5% water in Ar after the pretreatment. At this temperature, the catalyst was exposed to the gas mixture for 60 min followed by flushing of the catalyst for 30 min at the same temperature. Subsequently, the temperature was raised by 20°C/min to 600°C and desorption of species was monitored. More details on the experiments can be found in a previous publication.<sup>23</sup>

# Model

### Kinetic model

The kinetic model was developed by successively expanding the initial model with more reactions. As a first step, the adsorption and desorption of NH<sub>3</sub> were modeled using an NH<sub>3</sub>-TPD experiment. In this experiment, 250 ppm NH<sub>3</sub>, 10% O<sub>2</sub> and 5% H<sub>2</sub>O were present during the NH<sub>3</sub> adsorption step and only Ar in the following temperature ramp. Experiments have shown that the presence of O<sub>2</sub> or H<sub>2</sub> has no significant influence on the adsorption of NH<sub>3</sub> and these compounds are, therefore, not included in the model. The elementary steps and reactions included in the model are presented in Table 1. According to the model, ammonia adsorbs on two different sites, S1 and S2 with different adsorption energies.

Previously, we have shown by diffuse reflectance IR Fourier transform spectroscopy (DRIFTS) that the predominant surface species during H<sub>2</sub>-assisted NH<sub>3</sub>-SCR conditions are NH<sub>x</sub> species.<sup>6</sup> Although we know that even nitrates and nitrites exist on the surface during the reaction, we chose here to only include NH<sub>3</sub> adsorption in the model, since the purpose with the model is to use it for dosing of the reducing agents. Therefore, we aim for a simple model and fast calculations.

In the next step, oxidation of NH<sub>3</sub> with O<sub>2</sub> was modeled. Adsorbed NH<sub>3</sub> on the S1 site reacts with O<sub>2</sub> to N<sub>2</sub> reaction 5, or to NO, reaction 6 in Table 1. Reaction 5 (NH<sub>3</sub> oxidation to N2) is needed to describe the formation of N2 during NH<sub>3</sub> oxidation in the absence of H<sub>2</sub>. In the presence of H<sub>2</sub>, N<sub>2</sub> formation could also be formed by reaction 7 (SCR). Finally, the H<sub>2</sub>-assisted NH<sub>3</sub>-SCR reaction was modeled as one global reaction with a stoichiometry between NO, NH<sub>3</sub> and H<sub>2</sub> of 1:1:2. The stoichiometry has been established in a previous article on the basis of flow reactor experiments.<sup>23</sup> Moreover, the unselective oxidation of  $H_2$  with  $O_2$  is added to the model (reaction 8 in Table 1). In addition to production of NO and N2, formation of NO2 and N2O can be expected as side products during H<sub>2</sub>-assisted NH<sub>3</sub>-SCR over Ag/Al<sub>2</sub>O<sub>3</sub> catalysts. However, over the presulfated Ag/Al<sub>2</sub>O<sub>3</sub> sample, which was used for the reactor experiments, no formation of N2O was observed under any reaction conditions in the presence of water.<sup>23</sup> At 200°C, the formation of some NO<sub>2</sub> was observed.<sup>23</sup> However, since the NO<sub>2</sub> concentration never exceeded 15 ppm and, moreover, occurred only at that specific temperature, reactions including NO2 and N2O were omitted in the model.

Table 1. Reactions Included in the Model

Reaction number	Reaction		
r1	$NH_3 + S1 \rightarrow NH_3-S1$		
r2	$NH_3-S1 \rightarrow NH_3 + S1$		
r3	$NH_3 + S2 \rightarrow NH_3-S2$		
r4	$NH_3-S2 \rightarrow NH_3 + S2$		
r5	$2 \text{ NH}_3\text{-S1} + 1.5 \text{ O}_2 \rightarrow \text{N}_2 + 3 \text{ H}_2\text{O} + 2 \text{ S1}$		
r6	$2 \text{ NH}_3\text{-S1} + 2.5 \text{ O}_2 \rightarrow 2\text{NO} + 2\text{H}_2\text{O} + 2 \text{ S1}$		
r7	$2 \text{ NO} + 2 \text{ NH}_3\text{-S1} + 2.5 \text{ O}_2 + 4 \text{ H}_2 \rightarrow 2 \text{ N}_2$		
	$+7 H_2O + 2 S1$		
r8	$2 H_2 + O_2 \rightarrow 2 H_2O$		

Table 2. Reaction Rates, Pre-Exponential Factors and Activation Energies used in the Model

Reaction number	Reaction rate	Pre-exponential factor A	Activation energy E <sub>a</sub> [J/mol]
r1	$r1 = k_1 \cdot c_{NH3} \cdot (1 - \theta_{S1})$	355 <sup>a</sup>	0
r2	$r2 = k_2 \cdot \theta_{S1}$	$3.5 \cdot 10^{8}$ b	8.3·10 <sup>4 d</sup>
r3	$r3 = k_3 \cdot c_{NH3} \cdot (1 - \theta_{S2})$	$2030^{a}$	0
r4	$r4 = k_4 \cdot \theta_{S2}$	2.0·10 <sup>9</sup> b	6.3·10 <sup>4 d</sup>
r5	$r5 = k_5 \cdot \theta_{S1}$	$2.5 \cdot 10^{8}$ b,e	$1.43 \cdot 10^{5}$ d
r6	$r6 = k_6 \cdot \theta_{S1}$	$4.5 \cdot 10^{12}$ b,e	$2.09 \cdot 10^{5} \text{ d}$
r7	$r7 = k_7 \cdot c_{NO} \cdot \theta_{S1} \cdot c_{H2}$	$1.49 \cdot 10^{14}$ b,e	1.20·10 <sup>5</sup> d
r8	$r8 = k_8 \cdot c_{H2}$	$1.18 \cdot 10^{10}$ b,e	$1.20 \cdot 10^{5} \text{ d}$

am3/(s·kg cat), calculated by kinetic gas theory

### Parameters in the kinetic model

The expressions used for the reaction rates for each reaction are presented in Table 2 and the corresponding rate constants in the reaction rates are described by the Arrhenius equation

$$k_i = A_i(T) \cdot e^{\frac{-E_{a,j}}{RT}} \tag{1}$$

Temperature dependence of the pre-exponential factors is neglected in the model. To decrease the correlation between parameters in the model, some parameters were determined in advance. It was shown that many adsorption reactions are nonactivated or have low-activation energies. Therefore, the activation energy for adsorption of NH<sub>3</sub> on both adsorption sites (S1 and S2) is set to 0 kJ/mol, which is in line with other kinetic models. The pre-exponential factors for the adsorption reactions,  $A_{\rm ads}$  ( $A_1$  and  $A_3$ ) were determined by using kinetic gas theory where  $A_{\rm ads}$  is the pre-exponential factors for the adsorption reactions,  $A_{\rm ads}$  and  $A_3$  were determined by using kinetic gas theory

$$A_{ads} = \frac{N_A \cdot R \cdot T}{(2 \cdot \pi \cdot M \cdot R \cdot T)^{0.5}} \cdot A \cdot N_{cat} \cdot S(0)$$
 (2)

Here, a reference temperature of  $300^{\circ}$ C was used. Preexponential factors for reactions and desorption are typically in the range of  $10^{11}-10^{19}$  s<sup>-1</sup>.<sup>33</sup> Here we used for the preexponential factors of the desorption reactions r2 and r4 according to transition state theory

$$\frac{k_B \cdot T}{h} = 10^{13} s^{-1} \tag{3}$$

This value is adjusted by the number of sites ( $N_{\rm cat}$ ) to obtain the unit m<sup>3</sup>/(s·kg <sub>cat</sub>). All pre-exponential factors and activation energies are listed in Table 2.

# Reactor model

The monolith catalyst is modeled as five continuously stirred-tank reactors in series. The number of tanks is a compromise between computational time and accuracy. In the mass balance of the gases in each tank the difference between the molar flow from the previous tank and the flow to the next tank is equal to the mass transport from the gas bulk to the catalyst surface

$$F_{i,k-1} - F_{i,k} = k_{c,i,k} \cdot A_k \cdot \left( c_{g,i,k} - c_{s,i,k} \right) \tag{4}$$

All channels of the monolith are assumed to be identical. The mass transport from the bulk to the catalyst surface is equal to the adsorption, desorption and reactions occurring on the catalyst surface

$$k_{c,i,k} \cdot A_k \cdot \left( c_{g,i,k} - c_{s,i,k} \right) = \sum_{i} v_{i,j} \cdot r_{j,k} \cdot m_{wc,k} \tag{5}$$

Moreover, it is assumed that there are no radial concentration gradients, and no axial diffusion. Axially changes in the gas concentration over the catalyst are modeled by the number of tanks. Any mass-transfer limitations in the washcoat are neglected, and the mean surface coverage in each tank is used to model the surface reactions. The changes of the amount of one type of species on the catalyst surface are equal to the sum of all reaction of this species

$$N_{cat} \frac{\partial \theta_{i,k}}{\partial t} = \sum_{j} v_{i,j} \cdot r_{j,k} \tag{6}$$

The mass transfer from the bulk in the gas phase to the catalyst surface is modeled by the film model, where the mass transfer coefficient  $k_{c,i,k}$  is calculated from the Sherwood number

$$k_{c,i,k} = \frac{Sh \cdot D}{d_{channel}} \tag{7}$$

Where the diffusivity D is calculated according to

$$D = D_{ref} \cdot \left(\frac{T_{cat}}{T_{ref}}\right)^{1.75} \tag{8}$$

The reference diffusion coefficients were obtained from the Fuller correlation  $^{34}$  and have values of  $9.71\times10^{-5}$  m²/s for NO,  $8.31\times10^{-5}$  m²/s for O<sub>2</sub>,  $34.12\times10^{-5}$  m²/s for H<sub>2</sub>, and  $9.35\times10^{-5}$  m²/s for NH<sub>3</sub> at a reference temperature of  $400^{\circ}\text{C}$ . The Sherwood number Sh was here calculated from

$$Sh = 2.7652 \cdot (1 + 0.03349 \cdot Gz)$$
 (9)

Where the Graz number is obtained from

$$Gz = \frac{d_{\text{channel}}^2 \cdot v}{L_{\text{monolith}} \cdot D} \tag{10}$$

and  $\nu$  is the linear gas velocity. At all places in the monolith isothermal conditions are used since the temperature difference between the gas in the inlet of the monolith and the temperature in the monolith is less than 18.5°C at all studied temperatures. The maximum in temperature difference occurred between 300 and 400°C, where most of the  $H_2$  is combusted. The temperature used in the model is the monolith temperature.

# **Results and Discussion**

The conversion of NO increased slowly with the number of experiments as shown in Figure 1. In a previous investigation,

bmol/(s·kg cat)

calculated by transition state theory

dfitted for the model

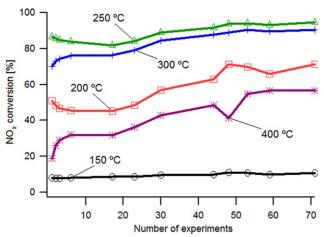


Figure 1. Conversion of NO<sub>x</sub> as a function of experiment number at different temperatures.

[Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

this increase has been explained by a gentile aging during the pretreatments and a part of each experiment at 500°C.<sup>23</sup> Each experiment consisted of activity tests at steady-state conditions between 150 and 500°C. For the modeling, a change in the conversion over time is a major challenge. Most of the experiments, which were included in the development of the model, were performed between the 17th and the 44th experiments. Between these experiments, the NO<sub>x</sub> conversion increased in the entire temperature range of the experiments. The most pronounced changes are observed at 200 and 400°C as shown in Figure 1. However, all experiments, in which the H<sub>2</sub> concentration was varied, were performed consecutively. The same is true for the variation of the NO and the variation of the NH<sub>3</sub> concentration. This procedure minimized the changes due to aging so that the aging does not need to be taking into account in the parameter fitting of the model. With these measures taken, a robust model was developed since it predicts the validation experiments well, which were performed after the 71st experiment.

# Ammonia Temperature Programmed Desorption (NH<sub>3</sub>-TPD) Experiments

An NH<sub>3</sub>-TPD experiment was used to model the NH<sub>3</sub> adsorption and desorption from the catalyst, and to determine the number of sites on which the reactions take place. As shown in Figure 2a, the model describes all features observed in the NH<sub>3</sub>-TPD well. For a good fit between experiment and model, two different adsorption sites were included in the model. One strong adsorption site, S1, and one weaker adsorption site, S2. The modeling results gave that the concentration of S1 and S2 sites is 0.04 and 0.2 mol/kg<sub>catalyst</sub>, respectively. As shown in Figure 2b, the strong adsorption site, S1, reaches full coverage fast due to the low concentration of this type of sites. The coverage of S2 starts to increase when the S1 sites are completely covered but reaches only 80% coverage at 100°C. The coverage of the S2 site is here very sensitive to the temperature and accounts for the small increase in NH<sub>3</sub> concentration, when the temperature increases from 98 to 100°C after about 1000 s. Moreover, the ammonia on the S2 site desorbs slowly at 100°C and gives rise to the tailing of the NH<sub>3</sub>-signal, which

4328

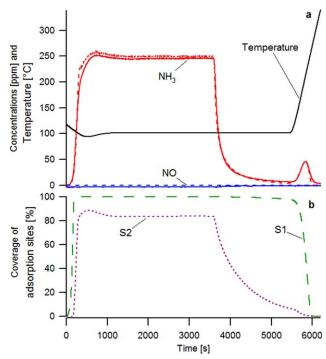


Figure 2. Measured (solid lines) and calculated (broken lines) concentrations and temperature (a), calculated coverage of S1 and S2 (b) during NH<sub>3</sub>-TPD.

Conditions: 250 ppm NH<sub>3</sub>, 10% O<sub>2</sub> and 5% H<sub>2</sub>O in Ar for 60 min at  $100^{\circ}$ C, 5% H<sub>2</sub>O in Ar for 30 min at  $100^{\circ}$ C, temperature ramp in 5% H<sub>2</sub>O in Ar,  $20^{\circ}$ C/min, GHSV = 33100 h<sup>-1</sup>. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

is observed after the NH3 supply is switched off. During the 30 min between NH<sub>3</sub> has been switched off and the start of the temperature ramp, the coverage of the S2 site decreases steadily. However, at the beginning of the temperature ramp, there is still some NH<sub>3</sub> adsorbed on S2. The ammonia coverage of S1 is constant during the flushing and drops during the temperature ramp. Since the catalyst consists of alumina supported silver species, it is possible to attribute silver and alumina sites to S1 and S2, respectively. However, according to Knözinger and Ratnasamy, 35 and Digne et al. 36 there are at least four different types of OH-groups with different properties on which molecules can adsorb on the alumina. Moreover, there will be differences depending on if a molecule adsorbs on a silver species or in the interface between a silver cluster and the alumina support.<sup>37</sup> However, in this model we used S1 and S2 sites in order to make the model simpler. In kinetic models, it is common to use coverage dependent activation barriers for desorption. The reason is either repulsive interaction between species or adsorption sites with a range of strength. For example Wilken et al.<sup>38</sup>, and Saha and Deng<sup>39</sup> determined the coverage dependent heats of adsorption over Cu-BEA and alumina, respectively. Sjövall et al. 40 used the coverage dependent activation energies according to

$$E_a = E_a(0) \cdot (1 - a_i \cdot \theta_i) \tag{11}$$

In this model, however, the best fit of the model to the experimental data is achieved when the activation energies for desorption from both sites (S1 and S2) are independent

of the coverage. Since we in this study use two adsorption sites, we also consider the effect of different strength of the sites. In the study by Wilken et al.<sup>38</sup> only one adsorption site was used.

### Ammonia oxidation

Figure 3a shows the concentrations of NH<sub>3</sub> and NO during NH<sub>3</sub> oxidation at different temperatures. Ammonia is adsorbed on the catalyst surface at 70°C and each time the temperature is increased some NH<sub>3</sub> desorbs up to 400°C. This is also the temperature, where NH<sub>3</sub> oxidation starts. Significant concentrations of NO, however, are only observed at 500°C. Formation of NO2 or N2O does not occur during the experiment. The part of the experiment without NH<sub>3</sub> oxidation is, thus, a validation of the parameters for NH<sub>3</sub> adsorption and desorption. There is a difference between the experimental and predicted results from the model for the NH<sub>3</sub> adsorption at 70°C, and the desorption peaks during the temperature increase to 100 and 150°C as shown in Figure 3a. This difference occurs since the parameters for NH<sub>3</sub> adsorption were obtained from a TPD experiment performed at 100°C. However, above 150°C where the catalyst is active for NO<sub>x</sub> reduction, the model describes desorption of NH<sub>3</sub> well. Figure 3b shows the calculated surface coverages of S1 and S2, which decrease stepwise with each temperature increase. Due to NH3 being present in the gas phase during the entire experiment, the model predicts some adsorbed NH<sub>3</sub> on S2 for temperatures below 250°C and on S1 below 400°C.

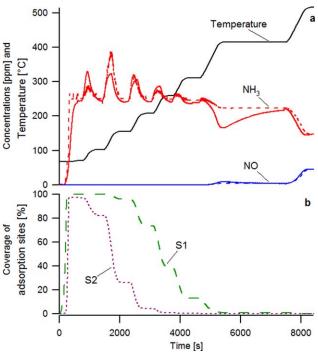


Figure 3. Oxidation of ammonia at different temperatures between 70 and 500°C, measured (solid lines) and calculated (broken lines) concentrations during NH<sub>3</sub> oxidation and temperature (a), and calculated surface coverage of S1 and S2 (b).

Conditions: 250 ppm NH<sub>3</sub>, 10% O<sub>2</sub> and 5% H<sub>2</sub>O in Ar, GHSV = 33100 h $^{-1}$ . [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

At 400°C, oxidation of NH<sub>3</sub> starts but only trace amounts of NO are observed. Although N2 has not directly been measured it is obvious from an N-balance that the major part of the oxidized NH<sub>3</sub> forms N<sub>2</sub>. At 500°C, substantial amounts of NO are formed and also the amount of formed N<sub>2</sub> increases. In the model, two reactions are introduced to describe NH<sub>3</sub> oxidation, i.e., the oxidation of NH<sub>3</sub> to N<sub>2</sub> (r5) and the oxidation of NH3 to NO (r6). Formation of N2O or NO<sub>2</sub> is not included, since these components were not observed in the experiments. With these assumptions the model describes the steady-state conditions during the oxidation of NH<sub>3</sub> well. However, the temporary decrease of the NH<sub>3</sub> concentration when increasing the temperature from 300 to 400°C cannot be described by the model as shown in Figure 3. In a previous publication, this temporary decrease of the NH<sub>3</sub> concentration was tentatively explained by a change in the oxidation state of the silver.<sup>23</sup> This phenomenon is more pronounced in the absence than in the presence of hydrogen and during the first NH<sub>3</sub> oxidation experiment succeeding an SCR experiment. A possible explanation for the different behavior in the absence and the presence of hydrogen is the fact, that silver oxides decomposes to metallic silver around 300°C in inert atmosphere. 41 Hydrogen as a reducing agent will clearly influence this process. Moreover, the oxidation of NH3 is impeded by H2 and increases with increasing O<sub>2</sub> concentration.<sup>23</sup> Since the oxidation of NH<sub>3</sub> occurs during NH<sub>3</sub>-SCR conditions only at 500°C, the dependencies on O2 and H2 are not included in the model to keep the model simple. Finally, it is interesting to note, that the formation of NO starts at the same temperature at which the model predicts that all NH<sub>3</sub> has desorbed from the surface. The co-occurrence of the surface coverage reaching zero and the start of the temporary decrease in the NH<sub>3</sub> concentration supports the explanation by the change in the oxidation state of the silver.

# Hydrogen-assisted ammonia-SCR

The Ag/Al<sub>2</sub>O<sub>3</sub> catalyst is very active for NO<sub>x</sub> reduction with NH<sub>3</sub> in the presence of H<sub>2</sub> as shown in Figure 4. Significant conversion of NO is observed from 150°C and a maximum of 93% is reached at 250°C. At higher

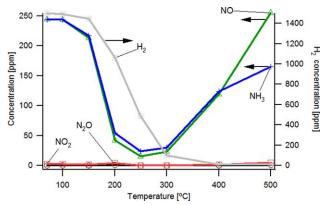


Figure 4. Concentrations of all relevant gases during H<sub>2</sub>-assisted NH<sub>3</sub>-SCR under steady-state conditions.

Experimental conditions: 250 ppm NO, 250 ppm NH<sub>3</sub>, 1500 ppm H<sub>2</sub>, 10% O<sub>2</sub>, 5% H<sub>2</sub>O in Ar.[Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

temperatures, the NO concentration is higher. At 500°C, the NO concentration after the catalyst is higher than in the inlet due to oxidation of NH<sub>3</sub> to NO. At all other studied temperatures the NO and NH3 concentrations follow each other closely and a ratio of one converted NO by one converted NH<sub>3</sub> has been established in a previous publication.<sup>23</sup> Moreover, NO, NH<sub>3</sub> and H<sub>2</sub> conversions start all at 150°C. All hydrogen is consumed at 400°C, where the NO concentration significantly increases, indicating that the lack of hydrogen limits the conversion of NO above 300°C. However, Ag/ Al<sub>2</sub>O<sub>3</sub> is not active for NO<sub>x</sub> reduction with only H<sub>2</sub> as reducing agent. 6,23 In a previous publication it was shown that there is a ratio between consumed NO and consumed H2 of 1:2 below 250°C.<sup>23</sup> Above this temperature, unselective oxidation of H<sub>2</sub> becomes increasingly important. As during the oxidation of NH3, the amounts of formed NO2 and N2O are extremely low. These gases are, therefore, not included in the model. Moreover, the reduction of NO with NH<sub>3</sub> and H<sub>2</sub> to N<sub>2</sub> and H<sub>2</sub>O is modeled as a single global reaction with a stoichiometry of NO: NH<sub>3</sub>: H<sub>2</sub> is equal to 1:1:2

$$2 \text{ NO} + 2 \text{ NH}_3 + 2.5 \text{ O}_2 + 4 \text{ H}_2 \rightarrow 2 \text{ N}_2 + 7 \text{ H}_2 \text{O}$$

# Variation of the hydrogen concentration

The conversion of NO is sensitive to the concentration of H<sub>2</sub>. As shown by the markers in Figure 5a and b, the NO and NH<sub>3</sub> concentrations decrease in a ratio of 1:1 with increasing H2 concentration at a fixed temperature, i.e., the NO<sub>x</sub> conversion increases with increasing H<sub>2</sub> concentrations in the feed. Figure 5c shows the concentration of H2 as a function of the temperature. Although, there is a large difference in the feed concentration of H2, hydrogen conversion starts at 150°C, independently of the inlet concentration. Moreover, complete H<sub>2</sub> conversion is in all experiments observed at 400°C, and at intermediate temperatures the conversion is independent of the inlet H<sub>2</sub> concentration within the studied concentration interval. The model captures all these features well as shown by the comparison of the model (lines) and the experimental data (markers) in Figure 5. In addition to the SCR reaction an unselective oxidation reaction of H<sub>2</sub> is included to account for the higher H<sub>2</sub> consumption above 250°C. However, there are some minor discrepancies. The model overestimates the NH3 oxidation at 500°C. This could be resolved by adding that H<sub>2</sub> impedes the oxidation of NH3 to the model, but would complicate the model. Moreover, the model somewhat overestimates the NO<sub>x</sub> conversion for 250 and 500 ppm H<sub>2</sub>. The model predicts that the surface coverage of S2 is independent of the inlet concentration of H<sub>2</sub>. In contrast to S2, the surface coverage of S1 decreases with increasing concentration in the inlet H<sub>2</sub> concentration between 200 and 300°C as shown in Figure 5d. This dependency of the surface coverage on the H<sub>2</sub> concentration is caused by differences in the actual NH<sub>3</sub> concentrations in the gas phase. In the context of the NH<sub>3</sub>-TPD, we attributed S1 and S2 to sites on silver and alumina, respectively. However, it has been shown that alumina is necessary for the SCR-reaction over Ag/Al<sub>2</sub>O<sub>3</sub>.6 Therefore, an unambiguous assignment of S1 and S2 to any physical sites on the catalyst is not possible.

# Variation of the NO concentration

In addition to the variation of the H<sub>2</sub> concentration also the NO concentration was varied keeping all other gas

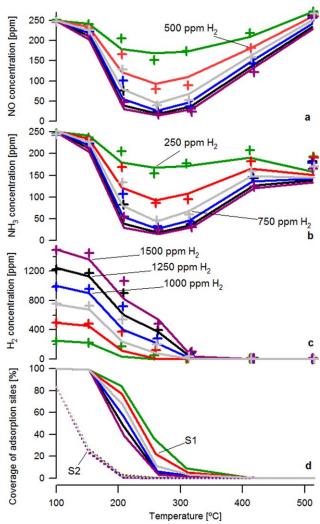


Figure 5. Concentrations of NO (a), NH<sub>3</sub> (b), and H<sub>2</sub> (c) during H<sub>2</sub>-assisted NH<sub>3</sub>-SCR with different concentrations of H2 during steady-state conditions between 100 and 500°C.

Experimental results are represented by points and calculated concentrations by the model as lines. Experimental conditions: 250 ppm NO, 250 ppm NH<sub>3</sub>, 250-1500 ppm  $H_2$ , 10%  $O_2$ , 5%  $H_2O$  in Ar. Calculated surface coverage of S1 (solid line) and S2 (broken line) (d). [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

concentrations constant as shown in Figure 6. The NO conversion increases with decreasing inlet NO concentration due to a higher ratio between NO and the reducing agents. The model describes this phenomenon very well. Only at 200°C, the model overestimates the NO and NH<sub>3</sub> conversion. Moreover, the model predicts that the coverage of the S2 site is independent of the NO concentration, while the coverage of the S1 site is higher with 125 ppm NO in the feed than with 250 or 375 ppm NO as shown in Figure 6d. This is reasonable, since the same trend is observed for the NH<sub>3</sub> concentration in the gas phase.

# Variation of the NH<sub>3</sub> concentration

The concentration of NH<sub>3</sub> has also been varied as another important parameter for H<sub>2</sub>-assisted NH<sub>3</sub>-SCR. As shown in Figure 7a and b, lowering the NH<sub>3</sub> concentration to a molar

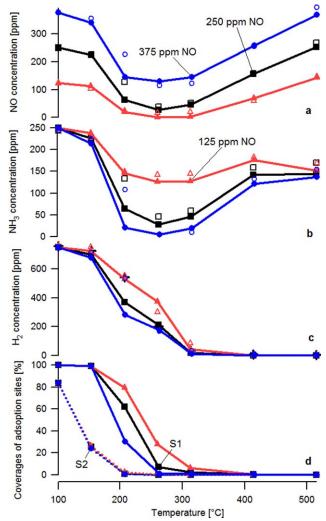


Figure 6. Concentrations of NO (a), NH $_3$  (b) and H $_2$  (c) during H $_2$ —assisted NH $_3$ -SCR with different concentrations of NO during steady state conditions between 100 and 500°C.

Experimental results are represented by markers and calculated concentrations by the model as lines. Experimental conditions: 125, 250 or 375 ppm NO, 250 ppm NH $_3$ , 750 ppm H $_2$ , 10% O $_2$ , 5% H $_2$ O in Ar. Calculated surface coverage of S1 (solid line) and S2 (broken line) (d). [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

ratio of one NH3 to two NO in the feed limits the NO conversion. However, increasing the ratio of NH<sub>3</sub> to NO above 1:1 is not beneficial for the NO conversion. This is unexpected after the results from the variation of the NO concentration. To explain this phenomenon it is important to notice, that the ratio between NH3 and NO as well as the ratio between NH<sub>3</sub> and H<sub>2</sub> changes when changing the NH<sub>3</sub> concentration and keeping all other parameters constant. It can, thus, be concluded that the H2 concentration limits the NOx conversion under these conditions. The model describes the NO<sub>x</sub> conversions with different inlet NH<sub>3</sub> concentrations well. Due to different NH3 concentrations in the outlet, the model also predicts different coverages on the two different adsorption sites. The dependence on the NH3 concentration of the S2 adsorption site was not seen when varying the concentrations of H<sub>2</sub> or NO (Figure 5d and Figure 6d). In these experiments, no major NH3 conversion occurred below

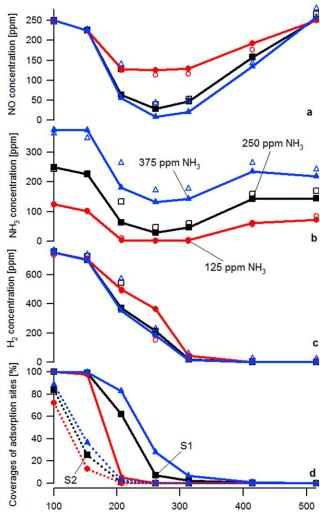


Figure 7. Concentrations of NO (a), NH<sub>3</sub> (b), and H<sub>2</sub> (c) during H<sub>2</sub>-assisted NH<sub>3</sub>-SCR with different concentrations of NH<sub>3</sub> during steady state conditions between 100 and 500°C.

Experimental results are represented by markers and calculated concentrations by the model as lines. Experimental conditions: 125, 250 or 375 ppm NH<sub>3</sub>, 250 ppm NO, 750 ppm H<sub>2</sub>, 10% O<sub>2</sub>, 5% H<sub>2</sub>O in Ar. Calculated surface coverage of S1 (solid line) and S2 (broken line) (d). [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

 $200^{\circ}$ C, where a significant coverage of the S2 site is predicted. Thus, the similar coverages in the previous experiments are due to similar NH<sub>3</sub> outlet concentrations.

# Validation of the model

The model was validated against three additional transient experiments, which were not included in the development of the model. These experiments were conducted at constant temperature (150, 200 and 250°C) where the supply of NO, H<sub>2</sub> and NH<sub>3</sub> to the feed separately was switched on and off after one long step with all compounds in the feed as shown in Figure 8a. All following steps lasted for 5 min. The model was developed with steady-state experiments, with exception for the NH<sub>3</sub>-TPD experiment. In the validation experiments with short steps, adsorption and desorption have a larger impact on the conversion of all gases. Figure 8 shows the transient experiment performed at 200°C; the temperature, at

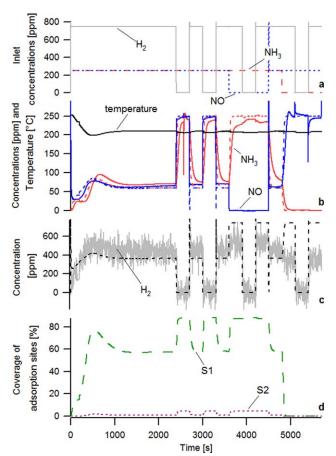


Figure 8. Feed gas composition (a) Experimental data (broken line) and calculated concentrations by the model (solid line) during a transient experiment switching H<sub>2</sub>, NO and NH<sub>3</sub> on and off at 200°C (b,c).

Calculated surface coverage during the experiment (d).[Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

which the fit between model and experiment is the worst. The light-off of the SCR-reaction occurs between 150 and 200°C. Therefore, the calculated concentrations are at 200°C especially sensitive to the parameters. In addition, the gradient of the conversion is steepest close to the light-off, which is also the case at 200°C. A small error in the temperature measurement will in this temperature region cause a clear deviation between the model and the experiment. Despite this difference during the fitting, the model describes the NO<sub>x</sub> conversion of this transient experiment very well. The model somewhat underestimates the adsorption and desorption of NH3 when the supply of different gas components is switched on and off. In addition, the conversion of hydrogen is somewhat inaccurate in the absence of ammonia in the last part of the experiment in Figure 8. This is due to the fact that at 200°C hydrogen is mainly consumed in the SCR reaction (r7) in the model. This reaction does not occur in the absence of NH<sub>3</sub>. At 200°C, the model predicts very lowsurface coverage's, between 0-5% for S2 and about 70% for S1 during NH<sub>3</sub>-SCR. When the hydrogen supply is switched off from the feed, the NH<sub>3</sub> coverage of S1 increases and reaches close to 90%. The same coverage of S1 is also predicted when both the supply of NO and H2 are switched off from the feed. In the presence of H2, NH3 and O2, however, the coverage is somewhat lower. This is interesting to note, since the NH<sub>3</sub> concentration decreased somewhat under these conditions in the experiment, but this detail is not reproduced by the model.

### Conclusions

A global kinetic model which describes hydrogen-assisted selective catalytic reduction of NO<sub>x</sub> with NH<sub>3</sub> over Ag/ Al<sub>2</sub>O<sub>3</sub> has been developed. The intention is that the model can be applied for dosing NH3 and H2 for a Ag/Al2O3 catalyst in a real automotive application. For this purpose, it is important that the model is simple to allow for fast calculations and, at the same time, accurately predicts the conversion of NO<sub>x</sub>. To achieve this goal, the model includes the adsorption and desorption of NH3 on two adsorption sites with different adsorption properties. Moreover, oxidation of NH<sub>3</sub> to N<sub>2</sub> and NO, and unselective oxidation of H<sub>2</sub> to water are included. The reduction of NO is described by a global reaction, with a stoichiometry between NO, NH<sub>3</sub> and H<sub>2</sub> of 1:1:2. The parameters of the model were obtained by fitting of an NH3-TPD experiment in the presence of O2, an NH3 oxidation experiment with 10% O2 in the adsorption step, and a series of H2-assisted NH3-SCR steady-state experiments in which the concentrations of H2, NO and NH3 were varied. With the obtained parameters and a set of six reactions it is possible to predict the conversion of NO<sub>x</sub> well even during transient experiments.

# **Acknowledgments**

This work is financially supported by the Danish Council for Strategic research and was performed at the Competence Center for Catalysis, Chalmers University of Technology. The collaboration with Haldor Topsøe A/S, Amminex and DTU is gratefully acknowledged.

### **Notation**

A = area for adsorption of one molecule

 $A_k$  = monolith wall area in tank k

 $A(T)_j$  = temperature-dependent pre-exponential factor for reaction i

= pre-exponential factor for adsorption reactions

 $c_{g,i,k}$  = concentration of species i in the gas phase of tank k

 $c_{s,i,k}$  = concentration of species i on the surface of tank k

D = diffusivity

 $d_{\text{channel}}$  = channel diameter

 $E_a$  = activation energy

 $E_a(0)$  = activation energy at zero surface coverage

 $F_{i,k}$  = molar flow of species i in tank k

Gz = Graz number

H = Planck constant

 $k_B$  = Boltzmann constant

 $k_{c,i,k}$  = mass-transfer coefficient of species i in tank k

 $k_j$  = rate constant for reaction j

 $L_{\text{monolith}}$  = length of monolith sample

M = molar mass

 $m_{wc,k}$  = mass of washcoat in tank k

 $N_A$  = Avogadro's constant

 $N_{\text{cat}}$  = number of active sites per mass washcoat

S(0) = Sticking coefficient

R = gas constant

 $r_{j,k}$  = rate of reaction j in tank k

Sh = Sherwood number

T = temperature

v =linear gas velocity in the monolith channel

### Greek letters

 $\alpha_i$  = coverage dependence for species i

 $v_{i,j}$  = Reaction coefficient of species i in reaction j

 $\theta_{Sx}^{(i)}$  = Coverage of adsorption site Sx

# **Literature Cited**

- Sun Q, Gao ZX, Chen HY, Sachtler WMH. Reduction of NO<sub>x</sub> with ammonia over Fe/MFI: Reaction mechanism based on isotopic labeling. *J Catal.* 2001;201(1):89–99.
- 2. Sjövall H, Olsson L, Fridell E, Blint RJ. Selective catalytic reduction of  $NO_x$  with  $NH_3$  over Cu-ZSM-5 The effect of changing the gas composition. *Appl Catal B Environ*. 2006;64(3-4):180–188.
- Kwak JH, Tonkyn RG, Kim DH, Szanyi J, Peden CHF. Excellent activity and selectivity of Cu-SSZ-13 in the selective catalytic reduction of NO<sub>x</sub> with NH<sub>3</sub>. J Catal. 2010;275(2):187–190.
- Uddin MA, Komatsu T, Yashima T. Catalytic properties of framework Fe<sub>3</sub><sup>+</sup> in MFI-type ferrisilicate Reaction-mechanism studies of co oxidation using an isotopic tracer technique. *J Catal.* 1994; 146(2):468–475.
- Richter M, Fricke R, Eckelt R. Unusual activity enhancement of NO conversion over Ag/Al<sub>2</sub>O<sub>3</sub> by using a mixed NH<sub>3</sub>/H<sub>2</sub> reductant under lean conditions. *Catal Lett.* 2004;94(1-2):115–118.
- Doronkin DE, Fogel S, Tamm S, et al. Study of the "Fast SCR"-like mechanism of H<sub>2</sub>-assisted SCR of NO<sub>x</sub> with ammonia over Ag/ Al<sub>2</sub>O<sub>3</sub>. Appl Catal B Environ. 2012;113-114:228–236.
- Kondratenko EV, Kondratenko VA, Richter M, Fricke R. Influence of O<sub>2</sub> and H<sub>2</sub> on NO reduction by NH<sub>3</sub> over Ag/Al<sub>2</sub>O<sub>3</sub>: A transient isotopic approach. *J Catal*. 2006;239(1):23–33.
- Breen JP, Burch R. A review of the effect of the addition of hydrogen in the selective catalytic reduction of NO<sub>x</sub> with hydrocarbons on silver catalysts. *Top Catal*. 2006;39(1-2):53–58.
- Brosius R, Arve K, Groothaert MH, Martens JA. Adsorption chemistry of NO<sub>x</sub> on Ag/Al<sub>2</sub>O<sub>3</sub> catalyst for selective catalytic reduction of NO<sub>x</sub> using hydrocarbons. *J Catal*. 2005;231(2):344–353.
- Chansai S, Burch R, Hardacre C, Breen J, Meunier F. Investigating the mechanism of the H<sub>2</sub>-assisted selective catalytic reduction (SCR) of NO<sub>x</sub> with octane using fast cycling transient in situ DRIFTS-MS analysis. *J Catal*. 2010;276(1):49–55.
- Shibata J, Takada Y, Shichi A, Satokawa S, Satsuma A, Hattori T. Ag cluster as active species for SCR of NO by propane in the presence of hydrogen over Ag-MFI. *J Catal.* 2004;222(2):368–376.
- Breen JP, Burch R, Hardacre C, Hill CJ. Structural investigation of the promotional effect of hydrogen during the selective catalytic reduction of NO<sub>x</sub> with hydrocarbons over Ag/Al<sub>2</sub>O<sub>3</sub> catalysts. J Phys Chem B. 2005;109(11):4805–4807.
- Kannisto H, Ingelsten HH, Skoglundh M. Aspects of the role of hydrogen in H<sub>2</sub>-assisted HC-SCR over Ag-Al<sub>2</sub>O<sub>3</sub>. *Top Catal*. 2009; 52(13-20):1817–1820.
- Sazama P, Capek L, Drobna H, et al. Enhancement of decane-SCR-NO<sub>x</sub> over Ag/alumina by hydrogen. Reaction kinetics and in situ FTIR and UV-vis study. *J Catal*. 2005;232(2):302–317.
- Shibata J, Shimizu K, Satokawa S, Satsuma A, Hattori T. Promotion effect of hydrogen on surface steps in SCR of NO by propane over alumina-based silver catalyst as examined by transient FTIR. *Phys Chem Chem Phys.* 2003;5(10):2154–2160.
- Zhang XL, Yu YB, He H. Effect of hydrogen on reaction intermediates in the selective catalytic reduction of NO<sub>x</sub> by C<sub>3</sub>H<sub>6</sub>. Appl Catal B Environ. 2007;76(3-4):241–247.
- Burch R, Breen JP, Hill CJ, et al. Exceptional activity for NO<sub>x</sub> reduction at low temperatures using combinations of hydrogen and higher hydrocarbons on Ag/Al<sub>2</sub>O<sub>3</sub> catalysts. *Top Catal*. 2004;30-31(1-4):19–25.
- Meunier FC, Breen JP, Zuzaniuk V, Olsson M, Ross JRH. Mechanistic aspects of the selective reduction of NO by propene over alumina and silver-alumina catalysts. *J Catal*. 1999;187(2):493–505.
- Creaser D, Kannisto H, Sjöblom J, Ingelsten HH. Kinetic modeling of selective catalytic reduction of NO<sub>x</sub> with octane over Ag-Al<sub>2</sub>O<sub>3</sub>. Appl Catal B Environ. 2009;90(1-2):18–28.
- Shimizu K, Shibata J, Satsuma A. Kinetic and in situ infrared studies on SCR of NO with propane by silver/alumina catalyst: Role of H<sub>2</sub>

- on  $O_2$  activation and retardation of nitrate poisoning. *J Catal.* 2006; 239(2):402-409.
- Guo Y, Chen J, Kameyama H. Promoted activity of the selective catalytic reduction of NO<sub>x</sub> with propene by H<sub>2</sub> addition over a metal-monolithic anodic alumina-supported Ag catalyst. *Appl Catal* A Gen. 2011;397(1-2):163–170.
- Tamm S, Valim N, Olsson L. The influence of hydrogen on nitrates during H<sub>2</sub>-assisted SCR over Ag/Al<sub>2</sub>O<sub>3</sub> catalysts - a DRIFT study. In press.
- Tamm S, Fogel S, Gabrielsson P, Skoglundh M, Olsson L. The effect of the gas composition on hydrogen assisted NH<sub>3</sub>-SCR over Ag/Al<sub>2</sub>O<sub>3</sub>. Appl Catal B Environ. 2013;136-137:168–176.
- Sjövall H, Blint RJ, Gopinath A, Olsson L. A Kinetic model for the selective catalytic reduction of NO<sub>x</sub> with NH<sub>3</sub> over an Fe-zeolitecatalyst. *Ind Eng Chem.* 2010;49(1):39–52.
- Lindholm A, Currier NW, Li JH, Yezerets A, Olsson L. Detailed kinetic modeling of NO<sub>x</sub> storage and reduction with hydrogen as the reducing agent and in the presence of CO<sub>2</sub> and H<sub>2</sub>O over a Pt/Ba/Al catalyst. J Catal. 2008;258(1):273–288.
- Colombo M, Nova I, Tronconi E, Schmeisser V, Bandl-Konrad B, Zimmermann L. NO/NO<sub>2</sub>/N<sub>2</sub>O-NH<sub>3</sub> SCR reactions over a commercial Fe-zeolite catalyst for diesel exhaust aftertreatment: Intrinsic kinetics and monolith converter modelling. *Appl Catal B Environ*. 2012;111:106–118.
- Nova I, Colombo M, Tronconi E, Schmeisser V, Weibel M. The NH<sub>3</sub> Inhibition effect in the standard scr reaction over a commercial Fe-zeolite catalyst for diesel exhaust aftertreatment: an experimental and modeling study. SAE Int J Engines. 2011;4(1):1822–1838.
- Backman H, Arve K, Klingstedt F, Murzin DY. Kinetic considerations of H<sub>2</sub> assisted hydrocarbon selective catalytic reduction of NO over Ag/Al<sub>2</sub>O<sub>3</sub> II. Kinetic modelling. Appl Catal A Gen. 2006; 304(1):86–92.
- Mhadeshwar AB, Winkler BH, Eiteneer B, Hancu D. Microkinetic modeling for hydrocarbon (HC)-based selective catalytic reduction (SCR) of NO<sub>x</sub> on a silver-based catalyst. *Appl Catal B Environ*. 2009;89(1-2):229–238.
- Sawatmongkhon B, Tsolakis A, Theinnoi K, York APE, Millington PJ, Rajaram RR. Microkinetic modelling for selective catalytic reduction (SCR) of NO<sub>x</sub> by propane in a silver-based automotive catalytic converter. Appl Catal B Environ. 2012;111-112:165–177.
- Boudart M, Djega-Mariadassou G. Kinetics of Heterogeneous Catalytic Reactions. Princeton, NJ: Princeton University Press; 1984.
- Olsson L, Sjövall H, Blint RJ. Detailed kinetic modeling of NO<sub>x</sub> adsorption and NO oxidation over Cu-ZSM-5. Appl Catal B Environ. 2009;87(3-4):200–210.
- Dumesic JA, Rudd DF, Aparicio LM, Rekoske JE, Treviño AA, eds. The Microkinetics of Heterogeneous Catalysis. Washington, DC: American Chemical Society; 1993. ACS Professional Reference Book.
- Fuller EN, Schettle PD, Giddings JC. A new method for prediction of binary gas-phase diffusion coeffecients. *Ind Eng Chem.* 1966; 58(5):19–27.
- Knözinger H, Ratnasamy P. Catalytic aluminas surface models and characterization of surface sites. Catal Rev Sci Eng. 1978;17(1):31– 70
- Digne M, Sautet P, Raybaud P, Euzen P, Toulhoat H. Use of DFT to achieve a rational understanding of acid-basic properties of gamma-alumina surfaces. J Catal. 2004;226(1):54–68.
- Hellman A, Groünbeck H. First-Principles Studies of NO<sub>x</sub> Chemistry on Ag<sub>n</sub>/α-Al<sub>2</sub>O<sub>3</sub>. J Phys Chem. C. 2009;113(9):3674–3682.
- Wilken N, Kamasamudram K, Currier NW, Li J, Yezerets A, Olsson L. Heat of adsorption for NH<sub>3</sub>, NO<sub>2</sub> and NO on Cu-Beta zeolite using microcalorimeter for NH<sub>3</sub>-SCR applications. *Catal Today*. 2010;151(3-4):237–243.
- Saha D, Deng SG. Characteristics of ammonia adsorption on activated alumina. J Chem Eng Data. 2010;55(12):5587–5593.
- Sjövall H, Blint RJ, Olsson L. Detailed kinetic modeling of NH<sub>3</sub> SCR over Cu-ZSM-5. Appl Catal B Environ. 2009;92(1-2):138–153.
- Li WX, Stampfl C, Scheffler M. Insights into the function of silver as an oxidation catalyst by ab initio atomistic thermodynamics. *Phys Rev B*. 2003;68(16).

Manuscript received Feb. 18, 2013, and revision received May. 6, 2013.